

Some useful identities for MOS IC design

SPG techteam – September 2011

MOS:

DC identities:

$$\text{Transconductance (KP)} = \mu_0 * C_{ox}$$

μ_0 = surface mobility ($\text{cm}^2/\text{V} - \text{sec}$)
 C_{ox} = Gate capacitance (farad/unit area)

$$C_{ox} = 0.0347/t_{ox} (\text{um}) \quad \text{fF/um}^2$$

V_t = $V_{t0} + \gamma [\sqrt{V_{bs} + 2\phi} - \sqrt{2\phi}]$
 V_{t0} = Extrapolated MOSFET threshold voltage at $V_{bs}=0$
 V_{bs} = Bulk to source reverse bias voltage
 V_t = Threshold voltage

$$2\phi = \text{Surface potential in strong inversion} = 2 * (KT/q) * \ln(N_a/n_i);$$

N_a = Substrate doping / cm^3
 n_i = Intrinsic concentration = $1.45E10 /\text{cm}^3$

γ = $\sqrt{(2 * \epsilon_s * q * N_a) / C_{ox}}$
 ϵ_s = dielectric constant of silicon
 γ = body effect constant.

* Note: γ can be used to find the substrate doping.

λ = parameter for slope of the I_{DS}/V_{DS} curve
 R_o = output impedance of the saturated MOSFET
 $= 1/(\lambda * I_{DS})$ (Ohms)

AC Identities:

For a saturated MOSFET:

$$C_{ox} * 0.33 = \text{gate to drain capacitance}$$

$$C_{ox} * 0.66 = \text{gate to source capacitance}$$

$$g_m = \text{sqrt}(2.0 * K_P * W/L * I_{DS})$$

$$A_{vol} = g_m * R_o$$

For a MOSFET in linear region:

$$C_{ox} * 0.5 = \text{gate to drain capacitance}$$

$$C_{ox} * 0.5 = \text{gate to source capacitance}$$

$$g_m = K_P * W/L * V_{DS}$$

$$R_o = 1/[K_P * W/L * (V_{gs} - V_t)]$$

Note: Add the overlap capacitance to the gate to drain/source capacitance. In addition the drain/source to substrate capacitance should be added.

The drain /source capacitances are depletion capacitances that are defined by:

$$C_{dep} = \text{sqrt}(1.602E-19 * 8.85E-12 * 11.9 * N * 1E6) / \text{sqrt}(V_{bi})$$

Here V_{bi} = built in voltage of the junction.

$$V_{bi} = K T / q * \ln[NA * ND / 1.9E20]$$

*Note: The junction (drain or source) is assumed to be an abrupt junction.
NA and ND in all the above identities are hole densities and electron densities
Sometimes called acceptor and donor densities.*