

Integrating $\text{sinc}^2(x)$ function from 0 to some number p

1.0 From Haykin S. (Communications Systems, 4th Edition):

$$\text{Sinc}(x) = 1 - 1/6(\pi x)^2 + 1/120(\pi x)^4 \dots \quad (1)$$

2.0 From the Web:

$$(2) \int \text{Sinc}^2(x) dx = \frac{1}{2}(\pi) = 1.57 \quad (\text{From } 0 \text{ to infinity})$$

3.0 Squaring (1) we get:

$$0.656x^8 - 2.66x^6 + 4.3x^4 - 3.3x^2 + 1 \quad (3)$$

4.0 Integrating (3) from 0 to πfT where f is the frequency and T is the time period of the PRBS waveform we get:

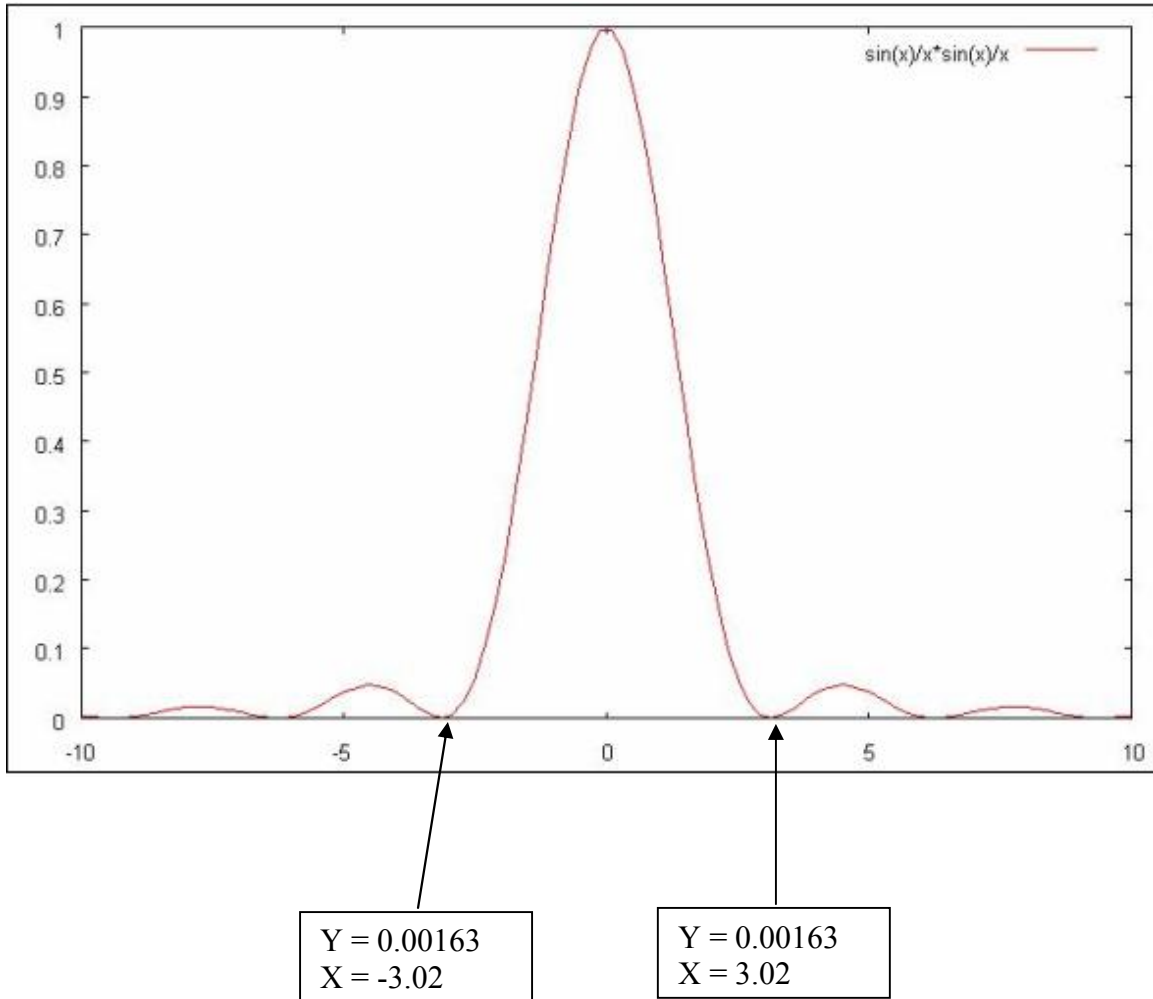
$$0.073x^9 - 0.38x^7 + 0.86x^5 - 1.1x^3 + x \quad (4)$$

5.0 Evaluating the polynomial above for $x = 0.12$. Frequency = 100 Mhz, T = 400ps we get:

$$\text{Power over } 0 \text{ to } 0.125 = 0.125 \text{ approximately}$$

By substituting the value of $x = 0.125$. For low values of x the power over the band is $1 \times x = \text{area}$. That is why the value of power is close to x.

The first null for the $\text{sinc}^2 x$ function occurs at: Please refer to Figure 1.0 below:



In the above figure the x values shown should be normalized to π and then the series representations above can be used. Thus it will be seen that when $x = 3.02$ is normalized by π , the series representation of $\sin^2 x$ will prove quite accurate. (Depends on the number of terms the user takes into account). I.e at $x=3.02/\pi$ the $y = 0.001$ approximately. The figure above shows that the first null occurs at a normalized x value of 0.96π).